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# Theoretical Study of the Reaction of Water with the 1,3 Dipoles Fulminic Acid and Acetonitrile Oxide. Concerted Reactions with a Proton Slide at the Transition State ${ }^{1}$ 

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#### Abstract

The ease of deformation of fulminic acid ( HCNO ) and acetonitrile oxide ( $\mathrm{CH}_{3} \mathrm{CNO}$ ), the formation of hydrogenbonded complexes with water, and the reaction pathway with water as nucleophile ( $\mathrm{RCNO}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{RC}(\mathrm{OH})=\mathrm{NOH}$ ) have been studied using the ab initio method. The calculations were carried out using Roothaan's LCAO-SCF-MO and the supermolecule technique, using Pople's STO-3G basis set. The reaction pathways were studied by allowing six angles and five bond distances to vary, using the distance $R$ between the carbon of the 1,3 dipole and the oxygen of the water molecule as reaction coordinate. Fulminic acid is most easily bent in the $E$ (or trans) direction and this is the configuration induced in the transition state as the water molecule approaches (thus determining the stereospecific nature of the reaction, as observed experimental1 y ). As the transition state is reached ( $R=1.85 \AA$ ) there is no energy barrier for the transfer of a proton from the oxygen of the attacking water molecule to that of the fulminic acid. The stereospecificity of the reaction thus ensures that the two oxygens are correctly oriented to facilitate this "proton slide". There are no intermediates on the reaction pathway which can thus be described as a concerted but asynchronous $(4 \pi+2 s)$ reaction. Acetonitrile oxide is less reactive (activation energy of 29.2 relative to $23.5 \mathrm{kcal} \mathrm{mol}^{-1}$ for fulminic acid) and the transition state is reached later with both more proton transfer and deformation of the 1,3 dipole. With HCNO two H -bonded complexes can be formed with water (which do not lie on the reaction pathway); the relative stabilities and the isomerization between the conformations of product hydroxyformaldoxime are also reported.


Nitrile oxides (1), which are propargyl-type 1,3 dipoles, react not only with unsaturated substrates ( $2 \pi$ systems) to give five-membered heterocycles, ${ }^{3}$ but also with nucleophilic reagents, including both anionic (such as $\mathrm{HO}^{-}, \mathrm{CH}_{3} \mathrm{O}^{-}, \mathrm{N}_{3}{ }^{-}$, etc.) and neutral ( $\mathrm{H}_{2} \mathrm{O}, \mathrm{ROH}, \mathrm{R}_{2} \mathrm{NH}$, etc.) examples. ${ }^{4}$ This latter addition leads to the formation of open-chain oximes as products.

The mechanism of the reaction of alkenes with 1,3 dipoles has been the subject of intensive study and there now appears to be agreement that this is generally a concerted reaction in which the bonds to the two termini of the dipolarophile are formed at or about the same time. ${ }^{3}$ The reaction of RCNO with nucleophiles occurs by attack at carbon; however, these reactions also appear to be stereospecific in that only one of the two possible oxime isomers in invariably formed. ${ }^{4}$ We have previously reported ${ }^{5}$ that this experimental result is confirmed in a model reaction-that of hydroxide ion $\left(\mathrm{HO}^{-}\right)$with fulminic acid (HCNO). In this case it was shown that the $Z$ form of the product was determined kinetically at the transition state-the configuration of the product was independent of any interaction between the oxygen of the 1,3 dipole and the incoming nucleophile (which was minimal).

In neutral solution ( $\mathrm{pH}<8$ ), water reacts with benzonitrile oxide ( $1, \mathrm{R}=\mathrm{Ph}$ ) and related 1,3 dipoles. ${ }^{4}$ The reaction is slow

( $t_{1 / 2}>100 \mathrm{~min}$ ) and was shown to be pH independent. Substituent effects suggest that water is also acting as a nucleophilic reagent.

We have now carried out a theoretical study on this reaction using both fulminic acid ( $1, \mathrm{R}=\mathrm{H}$ ) and acetonitrile oxide ( 1 , $\mathrm{R}=\mathrm{CH}_{3}$ ) as substrates. We were particularly interested in this case in the timing of proton-transfer relative to the movement of heavy atoms and in the possibility that both processes could be concerted.

## Methods of Calculation

The calculations were carried out by the ab initio method of Roothaan. ${ }^{6}$ In each case we have utilized the STO-3G basis set of Pople ${ }^{7 \mathrm{a}}$ with the GAUSSIAN-70 program. ${ }^{7 \mathrm{~b}}$ This basis set is sufficiently reliable for studying reactions between neutral molecules. Moreover, it is not necessary to include a limited configurational interaction in order to obtain qualitatively significant results, since the number of pairs of electrons is conserved in the course of reaction. We have adopted the


Figure 1. Potential energy hypersurface for the deformation of fulminic acid.


Figure 2. Optimized geometry of the $Z$, s-cis, s-trans form of hydroxyformaldoxime.
classical view of the supermolecule. Finally, charge centroids were obtained by the method of localization of Foster-Boys, ${ }^{8}$ a using Boyloc's ${ }^{8 \mathrm{~b}}$ program.

## Results and Discussion

Addition of Water to Fulminic Acid. A. Ability of Reactants to Undergo Deformation. The optimized geometries of the reactants have already been described. ${ }^{9}$ We have calculated the energy required to produce angular deformations in the fulminic acid molecule (since such geometric changes are induced in the reaction with nucleophiles). The angles $\Psi$ and $\Psi^{\prime}$ are defined as follows.


We have obtained energy values for different angles between +40 and $-40^{\circ}$. Using a second-order regression ${ }^{10}$ the energy potential of the surface, $E\left(\Psi, \Psi^{\prime}\right)$, in $\mathrm{kcal} \mathrm{mol}^{-1}$, can be expressed in the following quantitative way:

$$
\begin{aligned}
E\left(\Psi, \Psi^{\prime}\right)=-103754.016+0.005172 \Psi^{2}- & 0.006548 \Psi \Psi^{\prime} \\
& +0.013058 \Psi^{\prime 2}
\end{aligned}
$$

This equation describes an ellipsoid centered on the origin and with an axis of $\Psi=19.842^{\circ}$ relative to the main axis (Figure 1). The principal values of the second derivative matrix of this equation are 0.02848 (for the largest) and 0.00798 (for the second). This potential energy surface shows that the fulminic acid is linear in its equilibrium geometry. Such result has already been obtained by Houk, ${ }^{22}$ even with a $4-31 \mathrm{G}$ basis set. The Boys localization, where the CN bond is quasi-triple, gives


Figure 3. Relative energies ( $\mathrm{kcal} \mathrm{mol}^{-1}$ ) of the different forms of hydroxyformaldoxime.
a picture of HCNO in perfect agreement with this structure.

The grand axis of the ellipsoid corresponds to a deformation of fulminic acid toward the $E$ (or trans) form. A deformation of $10^{\circ}$ on this axis (comprising $\Psi=9.4^{\circ}$ and $\Psi^{\prime}=3.4^{\circ}$ ) only requires $0.80 \mathrm{kcal} \mathrm{mol}^{-1}$ while a deformation along the lesser axis (comprising $\Psi=-3.4^{\circ}$ and $\Psi^{\prime}=9.4^{\circ}$ ) requires 2.85 kcal $\mathrm{mol}^{-1}$. In summary, the $E$ (or trans) deformation with respect to the $\mathrm{C}=\mathrm{N}$ bond is far more readily achieved. Such observations have been also pointed out by Houk ${ }^{20,21}$ and are important in the reactivity of the fulminic acid. ${ }^{22}$

Using an analogous procedure we have calculated the energy associated with the angle ( $\xi$ ) of the water molecule. The following equation describes the energy (in $\mathrm{kcal}_{\mathrm{mol}}{ }^{-1}$ ) associated with deformation of this angle; the minimum arises when $\xi$ is $99.968^{\circ}$.

$$
\begin{aligned}
E(\xi)=-46890.725-10.069634 \xi
\end{aligned} \quad \begin{aligned}
& \quad+0.072348 \xi^{2}+0.0001466 \xi^{3}
\end{aligned}
$$

B. Isomers of Hydroxyformaldoxime. Hydroxyformaldoxime can exist in either $Z$ or $E$ configurations with respect to the $\mathrm{C}_{2} \mathrm{~N}_{3}$ double bond and in the conformations s -cis and s trans with respect to the single bonds $\mathrm{O}_{1} \mathrm{C}_{2}$ and $\mathrm{N}_{3} \mathrm{O}_{4}$. We have optimized its geometry while maintaining constant the CH and OH bond lengths ( $R_{\mathrm{CH}}=1.07 \AA$ and $R_{\mathrm{OH}}=0.99 \AA$ ). As an example, we have given in Figure 2 the structure obtained for the $Z$, s-cis, s-trans form.

The bond lengths remain constant in each form and the valence angles vary by no more than a few degrees. In Figure 3 we have compared the relative energies of the different structures of hydroxyformaldoxime. The respective stabilities depend on the equilibrium between the repulsive interactions between adjacent hydrogens and hydrogen-oxygen or hydro-gen-nitrogen attractions.

We have also studied the s-cis-s-trans isomerization for the hydroxyformaldoxime in the $Z$ configuration. Two mechanisms of isomerization are generally proposed ${ }^{11}$ for this type of reaction: an out-of-plane rotation of the $\mathrm{O}-\mathrm{H}$ or an inversion in the molecular plane. In Figure 4 are given definitions of the structural parameters considered. Tables I and II give the total energies calculated for the two reaction pathways for isomerization.

We have obtained an analytical form ${ }^{10}$ for these hypersurfaces using a development of a Fourier series in two dimensions, including in each direction in space ( $\varphi$ and $\varphi^{\prime}$ for rotation, $\delta$
${ }^{a}$ Activated complex.


Rotalion
(hereq $=\varphi^{\circ}=0$ )


Inversion
(here $\delta=\delta^{\prime}=100^{\circ}$ )

Figure 4. Geometric parameters for the isomerization s-cis-s-trans form.


Figure 5. Potential energy diagram for the isomerization s-cis-s-trans of hydroxyformaldoxime by an out-of-plane rotation.


Figure 6. Potential energy diagram for the isomerization s-cis-s-trans of hydroxyformaldoxime by an in-plane inversion mechanism.
and $\delta^{\prime}$ for inversion) five even functions ( $1.0, \cos \alpha, \cos 2 \alpha, \cos$ $3 \alpha, \cos 4 \alpha$, with $\alpha=\varphi, \varphi^{\prime}, \delta$, or $\delta^{\prime}$ ) and three uneven functions $(\sin \alpha, \sin 2 \alpha$, and $\sin 3 \alpha)$. The development of the series then contains 64 basic functions; the multiple regression coefficients obtained are better than 0.992 and the residual variance is less than 0.8 kcal . In Figures 5 and 6 are given two-dimensional illustrations of the potential energy hypersurfaces. The main points are summarized in Figure 7; we have included in the same figure the associated energies. The structures I-IV are minima while IX-XII and XVI-XIX are minimax and structures XIH-XV are maxima on the potential energy hypersurfaces.

In summary, rotations about the single bonds $\mathrm{C}_{2}-\mathrm{O}_{1}$, and $\mathrm{N}_{3}-\mathrm{O}_{4}$ are facile nuclear motions and require activation
 These results are in line with other reported studies ${ }^{12}$ on s -cis-s-trans isomerization. On the other hand, the inversion barriers are considerably higher ( $60-80 \mathrm{kcal} / \mathrm{mol}$ ). Such re-

Table II. Isomerization s-Cis-s-Trans of ( $Z$ )-Hydroxyformaldoxime. Mechanism of In-Plane Inversion ( $E=-240 . x x x \mathrm{au}$ )

|  | $\delta^{\prime}$, deg |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\delta$, deg | 100 | 120 | 140 | 160 | 180 | 200 | 220 | 240 | 260 |
| 100 | 0.48900 (III) | 0.47702 | 0.43721 | 0.38622 | $0.358868^{\text {a }}$ (XVI) | 0.37905 | 0.43035 | 0.47545 | 0.49325 (IV) |
| 120 | 0.48043 | 0.47048 | 0.42995 | 0.37846 | 0.35029 | 0.37122 | 0.42276 | 0.46808 | 0.48463 |
| 140 | 0.45227 | 0.43980 | 0.40012 | 0.34725 | 0.31868 | 0.34000 | 0.39207 | 0.43706 | 0.45364 |
| 160 | 0.41865 | 0.40585 | 0.36453 | 0.31266 | 0.28409 | 0.30580 | 0.35748 | 0.40289 | 0.41933 |
| 180 | $0.39915^{\text {a }}$ (XVIII) | 0.38827 | 0.34851 | 0.29764 | 0.26966 (XV) | 0.29175 | 0.34345 | 0.38877 | $0.4059^{a}$ (XIX) |
| 200 | 0.41022 | 0.40165 | 0.36275 | 0.31280 | 0.28583 | 0.30886 | 0.36068 | 0.40568 | 0.42247 |
| 220 | 0.44165 | 0.43450 | 0.39535 | 0.34793 | 0.32136 | 0.34588 | 0.39980 | 0.44183 | 0.45846 |
| 240 | 0.46851 | 0.46426 | 0.42827 | 0.37920 | 0.35466 | 0.37944 | 0.43071 | 0.47501 | 0.49109 |
| 260 | 0.47767 (II) | 0.46887 | 0.43497 | 0.38862 | $0.34741^{a}$ (XVII) | 0.39339 | 0.44367 | 0.48596 | 0.50159 (I) |

${ }^{a}$ Activated complex.


Figure 7. The s-cis-s-trans isomerization of $Z$-formaldoxime ( $\Delta E$ in kcal $\mathrm{mol}^{-1}$ ).
sults are probably at least in part an artifact of the STO-3G basis set, which is known to overestimate the activation energy of the inversion process. ${ }^{23}$
C. Water-Fulminic Acid Complexes. The addition reaction of fulminic acid and water may be preceded by the formation of a molecular complex. The electrostatic potential map ${ }^{13}$ $(V(\mathrm{M}))$ for fulminic acid (Figure 8) shows the presence of an electrophilic region $(V>0)$ about the hydrogen atom and a nucleophilic region $(V<0)$ at the oxygen atom. The minima of electrostatic potential are placed on the perimeter of the base of a cone whose apex is at the oxygen atom and whose axis of revolution is the axis HCNO. The aperture angle of this cone is $48.2^{\circ}$ and the distance between the oxygen and the potential minima is $2.21 \AA$. This circumference then has an electrostatic potential of $-63.3 \mathrm{kcal} \mathrm{mol}^{-1}$.

The potential energy curve calculated is given in Figure 9. The displacement of the water molecule about the fulminic acid molecule leads at all times to stabilization, and the change from one complex to the other results in the rotation of the water molecule during its displacement along the axis of HCNO. The general characteristics of the complexes are given in Table III.

Using the supermolecule technique, we have sought the existence of molecular complexes. Keeping the internal geometry of the isolated reactants unchanged, we have displaced a water molecule about the fulminic acid molecule searching for the relative orientations which were most favorable for the two molecules. In each case, the planar structure is the most stable. Two stable molecular complexes are obtained, one resulting from nucleophilic attack by water on the hydrogen atom


Figure 8. Potential energy diagram of the fulminic acid molecule and the complexation sites of water.

Table III. Characteristics of the Water-Fulminic Acid Complexes

| complex | $r_{\mathrm{O} \cdots \mathrm{H},}, \AA$ | $\Delta H_{\mathrm{f}, \mathrm{kcal} / \mathrm{mol}}$ | $\mu, \mathrm{D}$ | $t^{*} \mathrm{H}_{2} \mathrm{O}, \mathrm{c}^{-}$ |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{HCNO}$ | 1.75 | -8.4 | 6.5 | -0.046 |
| $\mathrm{HCNO} \cdots \mathrm{H}_{2} \mathrm{O}$ | 1.90 | -4.5 | 3.0 | 0.031 |

of the fulminic acid and possessing $C_{2 v}$ symmetry, the other resulting from electrophilic attack of water on the oxygen atom of fulminic acid with an angle of attack of $70^{\circ}$. In Figure 8 we have represented the nuclear structures of the two complexes and superimposed them on the electrostatic potential map of the fulminic acid molecule. As previously noted by others, ${ }^{14}$ the electrostatic potential map is a valuable tool in searching for complexation sites.

For the molecular complexes we have allowed relaxation of fulminic acid and water angles. Such a freedom does not modify the angles more than $2^{\circ}$ and improves the energy by less than $3 \times 10^{-5} \mathrm{au}$.
The results recall the heats of formation and the charge transfer obtained in the hydrogen-bonded complexes $\mathrm{H}_{2} \mathrm{O} \cdots$ $\mathrm{H}_{2} \mathrm{O}^{15}$ and $\mathrm{H}_{2} \mathrm{O} \cdots \mathrm{HF}^{16}$ In sum, the oxygen atom acts as a nucleophilic center and the hydrogen atom as an electrophilic center. The carbon atom, which is also electrophilic ( $\Delta E=1.6$ $\mathrm{kcal} \mathrm{mol}^{-1}$ ), does not give rise to a minimum in the potential energy hypersurface. Because of this, the molecular complexes between water and fulminic acid do not appear on the reaction pathway for addition (formation of hydroxyformaldoxime).
d. Reaction Pathway for Addition, The reaction pathway for the addition of water to fulminic acid has been calculated as a function of the parameters listed (defined in Figure 10): $\alpha$, $\mathrm{O}_{1} \mathrm{C}_{2} \mathrm{~N}_{3}$ angle; $\beta, \mathrm{H}_{7} \mathrm{C}_{2} \mathrm{~N}_{3}$ angle; $\gamma, \mathrm{O}_{4} \mathrm{~N}_{3} \mathrm{C}_{2}$ angle; $\theta, \mathrm{H}_{6} \mathrm{O}_{1} \mathrm{C}_{2}$ angle; $\mu, \mathrm{H}_{5} \mathrm{O}_{1} \mathrm{C}_{2}$ angle; $\nu, \mathrm{H}_{6} \mathrm{O}_{4} \mathrm{~N}_{3}$ angle; $r, \mathrm{O}_{1} \mathrm{H}_{6}$ bond length; $r^{\prime}, \mathrm{H}_{6} \mathrm{O}_{4}$ distance; $r_{\mathrm{CN}}, \mathrm{C}_{2} \mathrm{~N}_{3}$ bond length; $r_{\mathrm{NO}}, \mathrm{N}_{3} \mathrm{O}_{4}$


Figure 9. Structure and energy of the water-fulminic acid molecular complexes.
Table IV. Structure and Energy Characteristics along the Reaction Pathway for the Reaction between HCNO and $\mathrm{H}_{2} \mathrm{O}$

| $R, \AA$ | $\alpha, \mathrm{deg}$ | $\beta, \mathrm{deg}$ | $\gamma, \mathrm{deg}$ | $\mu, \mathrm{deg}$ | $\theta, \mathrm{deg}$ | $\nu, \mathrm{deg}$ | $r_{\mathrm{O}_{1} \mathrm{~N}_{2}, \AA}, r_{\mathrm{N}_{2} \mathrm{C}_{3}, \AA} \AA$ | $r, \AA$ | $r^{\prime}, \AA$ | $E, \mathrm{av}$ |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\infty$ |  | 180 | 180 |  |  |  | 1.30 | 1.16 | 0.99 |  | -240.368084 |
| $2.73 a$ | 180 | 180 | 180 | 130 | 130 | 8 | 1.30 | 1.16 | 0.99 | 5.87 | -240.371452 |
| 2.50 | 115 | 175 | 175 | 155 | 101 | 50 | 1.30 | 1.16 | 0.99 | 3.85 | -240.357193 |
| 2.25 | 112 | 170 | 170 | 155 | 101 | 54 | 1.30 | 1.16 | 0.99 | 3.43 | -240.350634 |
| 2.10 | 110 | 165 | 165 | 155 | 101 | 58 | 1.31 | 1.17 | 0.99 | 3.15 | -240.343113 |
| 2.05 | 110 | 160 | 160 | 155 | 101 | 61 | 1.31 | 1.18 | 0.99 | 3.01 | -240.339032 |
| 2.00 | 110 | 155 | 155 | 155 | 101 | 64 | 1.32 | 1.19 | 0.99 | 2.88 | -240.334366 |
| 1.95 | 110 | 152 | 151 | 154 | 101 | 67 | 1.32 | 1.20 | 0.99 | 2.76 | -240.329430 |
| 1.90 | 110 | 150 | 147 | 153 | 101 | 69 | 1.33 | 1.21 | 0.99 | 2.64 | -240.324698 |
| $1.85 b$ | 109 | 147 | 143 | 150 | 101 | 72 | 1.34 | 1.22 | 0.99 | 1.88 | -240.320695 |
| 1.80 | 109 | 134 | 120 | 103 | 78 | 100 | 1.34 | 1.22 | 1.58 | 0.99 | -240.385176 |
| 1.70 | 109 | 130 | 118 | 103 | 80 | 100 | 1.36 | 1.24 | 1.61 | 0.99 | -240.449213 |
| 1.60 | 116 | 125 | 117 | 103 | 80 | 100 | 1.39 | 1.27 | 1.85 | 0.99 | -240.459983 |
| $1.40^{c}$ | 121 | 120 | 115 | 106 | 82 | 100 | 1.41 | 1.29 | 1.93 | 0.99 | -240.488983 |

${ }^{a}$ Complex. ${ }^{b}$ Transition state. ${ }^{c}$ Product.
bond length; $R, \mathrm{O}_{1} \mathrm{C}_{2}$ distance. The distance $R$ has been chosen as the reaction coordinate.

The calculations show that at all points on the reaction pathway all of the atoms remain in the same plane. In Table IV we have given the structural characteristics and energetics of the reaction pathway. Using the basis set STO-3G, the activation barrier, relative to the isolated reactants, is 23.5 kcal $\mathrm{mol}^{-1}$ and the heat of reaction $-82.1 \mathrm{kcal} \mathrm{mol}{ }^{-1}$.

In summary, the reaction occurs in two phases. The first is deformation of the fulminic acid in the $E$ (trans) mode as the water approaches the carbon atom; this determines that the product will have the $Z$ configuration (as experimentally observed in all analogous reactions). ${ }^{4}$ Thus the transition state is i . The second is transfer of the hydrogen atom $\mathrm{H}_{6}$ from the oxygen $\mathrm{O}_{1}$ toward the atom $\mathrm{O}_{4}$, thus leading to the hydroxyformaldoxime of structure $Z$ (s-trans $\mathrm{O}_{1} \mathrm{C}_{2}$, s-cis $\mathrm{N}_{3} \mathrm{O}_{4}$ ) (ii).

i

ii


Figure 10. Geometric parameters for the addition of water to fulminic acid.

At the transition state the angles $\Psi$ and $\Psi^{\prime}$ have the values of 33 and $37^{\circ}$, respectively. Such a deformation of the isolated fulminic acid molecule requires $15.5 \mathrm{kcal} \mathrm{mol}^{-1}$. At the same time, the angle $\mathrm{HOH}(\xi)$ of the water molecule changes from 100 to $109^{\circ}$; this deformation requires $2.3 \mathrm{kcal} \mathrm{mol}^{-1}$. Thus we can say that these deformations alone account for 17.8 kcal $\mathrm{mol}^{-1}$, which represents $76 \%$ of the total height of the activation barrier.

We observe that the easier deformation mode of fulminic acid corresponds also to the molecular distortion during the addition of $\mathrm{H}_{2} \mathrm{O}$ to HCNO . Such result has been also pointed out by Houk ${ }^{22}$ in the nucleophilic addition to acetylenes. Nevertheless, this is not a general rule; otherwise the approach


Figure 11. Evolution of the potential energy hypersurface along the reaction pathway for the reaction of HCNO with $\mathrm{H}_{2} \mathrm{O}$. Zero level with respect to reactants (kcal/ $\mathrm{mol}^{-1}$ ): (a) 14.9; (b) -8.2 ; (c) -13.3 ; (d) -17.0 .
of diazomethane on ethylene would be in two parallel planes and not as found by some of us. ${ }^{24}$

Figure 11 shows four sections in the potential energy hypersurface which correspond to the parameters $R, r$, and $r^{\prime}$. It should be noted that at $R=1.85 \AA$ a corridor is created in the hypersurface which permits the transfer of the hydrogen from one oxygen to the other. This corridor is a nearly flat valley connecting the point $R=1.85 \AA, r=1.00 \AA$, and $R^{\prime}=$ $2.50 \AA$ with the transition state $R=1.85 \AA, r=1.00 \AA$, and $r^{\prime}=1.88 \AA$.

The Boys localization method ${ }^{8}$ permits us to follow the electronic reorganization along the reaction pathway. On Figure 12, we have given the charge centroids calculated at different points on the pathway. The approach route followed by the water molecule is along the axis of one of its lone pairs. The effect of the dipolar deformation leads to the formation of a lone pair on the central nitrogen from the original triple bond $\mathrm{C}_{2} \mathrm{~N}_{3}$. The rest of the electronic rearrangements occur after the transition state. Then the hydrogen $\mathrm{H}_{6}$ is displaced progressively, passing from one lone pair on the oxygen $\mathrm{O}_{1}$ to another lone pair on the oxygen $\mathrm{O}_{4}$. In parallel, the formation of the intersystem $\sigma$ bond $\mathrm{O}_{1} \mathrm{C}_{2}$ occurs. The electronic reorganization is summarized as follows:

$$
\begin{gathered}
\mathrm{n}\left(\mathrm{O}_{1}\right) \rightarrow \sigma\left(\mathrm{C}_{1} \mathrm{O}_{2}\right) \\
\pi\left(\mathrm{N}_{3} \mathrm{C}_{2}\right) \rightarrow \mathrm{n}\left(\mathrm{~N}_{3}\right) \\
\mathrm{n}\left(\mathrm{O}_{4}\right) \rightarrow \sigma\left(\mathrm{O}_{4} \mathrm{H}_{6}\right) \\
\sigma\left(\mathrm{O}_{1} \mathrm{H}_{6}\right) \rightarrow \mathrm{n}\left(\mathrm{O}_{1}\right)
\end{gathered}
$$

Eight electrons in all are implicated in this reorganization; these occur in a cyclic way as shown schematically in Figure 13.

In Table V are given the changes in the overlap populations ( $P_{\mathrm{AB}}$ ) along the reaction pathway. According to the usual method ${ }^{17,18}$ we have transposed the magnitudes in terms of the energies of the bonds ( $E_{\mathrm{AB}}$ ) using the following relationships:

$$
\begin{gathered}
E_{\mathrm{CO}}=1279.20 P_{\mathrm{CO}^{3}}-516.12 P_{\mathrm{CO}^{2}}+339.25 P_{\mathrm{CO}} \\
E_{\mathrm{NO}}=571.77 P_{\mathrm{NO}}+120.97 P_{\mathrm{NO}}{ }^{2}+231.50 P_{\mathrm{NO}} \\
E_{\mathrm{OH}}=435.48 P_{\mathrm{OH}}
\end{gathered}
$$

The validity of these expressions has been discussed previously. ${ }^{18}$ Using these values it is possible to estimate the degree of evolution of the bonds in the transition state ( $T_{\mathrm{AB}}$ ) using the following relationship:

$$
T_{\mathrm{AB}}^{\neq}=100 \frac{E_{\mathrm{AB}}(\neq)-E_{\mathrm{AB}}(\text { reactant })}{E_{\mathrm{AB}}(\text { product })-E_{\mathrm{AB}}(\text { reactant })}
$$

These quantities are also included in Table $V$. It is noted that at the transition state the $\mathrm{C}_{2} \mathrm{~N}_{3}$ bond has changed to an important degree while the $\mathrm{O}_{1} \mathrm{C}_{2}$ bond is weak and the bond $\mathrm{O}_{4} \mathrm{H}_{6}$ is almost nonexistent.

If the asynchronization of the reaction is defined as

$$
A=100 \frac{T^{\ddagger} \mathrm{C}_{2} \mathrm{O}_{1}-T^{\ddagger} \mathrm{O}_{4} \mathrm{H}_{6}}{T^{\ddagger} \mathrm{C}_{2} \mathrm{O}_{1}}+T^{\ddagger} \mathrm{O}_{4} \mathrm{H}_{6}
$$

then it can be calculated as $96.6 \%$. Since there is no intermediate on the reaction pathway, the reaction can thus be defined as being concerted but asynchronous.

Finally we have observed that the charge transferred from the water molecule to fulminic acid is 0.15 electrons in the transition state. This charge transfer is clearly weaker than in the case of the addition of hydroxide ion to fulminic acid, ${ }^{5}$ but it occurs in the same direction (i.e., in that expected for a nucleophile addition).

## Addition of Water to Acetonitrile Oxide

In order to obviate the formation of hydrogen-bonded complexes between the nucleophile and the $\mathrm{H}_{7} \mathrm{C}_{2}$ of fulminic acid (noted above with water and also reported ${ }^{5}$ with hydroxide ion) we have also studied the reaction of water with acetonitrile oxide (methyl fulminate). We were also interested in determining the effect of a substituent both on the deformability of the nitrile oxide and on the energy barrier for reaction.

We have as previously calculated the form of the hypersurface of the potential energy for deformation of the isolated acetonitrile oxide molecule. The analytical form ${ }^{10}$ at this hypersurface as a function of the angles of deformation $\Psi$ and $\Psi^{\prime}$ is as follows (in kcal $\mathrm{mol}^{-1}$ ):

$$
\begin{aligned}
E\left(\Psi, \Psi^{\prime}\right)=-127966.33+ & 0.00603 \Psi^{2} \\
& -0.00726 \Psi \Psi^{\prime}+0.01308 \Psi^{\prime 2}
\end{aligned}
$$

Table V. Overlap Populations, Bond Energies, and Degree of Evolution of Bonds at Several Points along the Reaction Pathway for WaterFulminic Acid Reaction

|  | $\mathrm{O}_{1}-\mathrm{H}_{6}$ | $\mathrm{O}_{1}-\mathrm{C}_{2}$ | $\mathrm{C}_{2}-\mathrm{N}_{3}$ | $\mathrm{N}_{3}-\mathrm{O}_{4}$ | $\mathrm{O}_{4}-\mathrm{H}_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Overlap Populations |  |  |  |  |  |
| reactants | 0.2539 | 0.0000 | 0.7463 | 0.2161 | 0.0000 |
| transition state | 0.2692 | 0.0446 | 0.6199 | 0.2048 | 0.0008 |
| product | 0.0066 | 0.2766 | 0.4935 | 0.2223 | 0.2477 |
| Bond Energies ( $\mathrm{kcal} \mathrm{mol}^{-1}$ ) |  |  |  |  |  |
| reactants | 110.6 | 0.0 | 207.5 | 61.5 | 0.0 |
| transition state | 117.2 | 14.2 | 158.4 | 57.4 | 0.3 |
| product | 2.9 | 81.4 | 114.1 | 63.7 | 107.9 |
| Degree of Bond Evolution (\%) ${ }^{\text {(\%) }}$ |  |  |  |  |  |
| transition state |  | 17.5 | 52.6 |  | 0.3 |


$R=2.501$ $\left(r=0.98 \AA_{i} ; r^{\prime}=3.85 A\right)$

$\mathrm{R}=1.80 \AA$
$\left(r=0.08 i ; r^{\prime}=2.24 A\right)$

$\mathrm{R}=1.80 \AA$
$\left(r=1.60 \AA ; r^{\prime}=0.80 \AA\right.$ )

$R=1.85 \AA(\neq)$
( $r=0.99 A^{\prime} r^{\prime}=2.50 \AA$ )

$R=1.80 \AA$
$\left(r=0.98 \AA ; r^{\prime}=1.40 \AA\right)$

$R=1.40 \dot{A}(111)$
( $r=1.93 \AA ; r^{\prime}=0.08 \AA$ )

Figure 12. Evolution of the charge centroids along the reaction coordinate for addition of $\mathrm{H}_{2} \mathrm{O}$ to HCNO . (The point of view is rotated by $30^{\circ}$ for convenience.)

This expression is in the form of an ellipsoid, centered at the origin, whose major axis is inclined at $22.92^{\circ}$ to the axis of $\Psi$. The principal values of the second derivative matrix are respectively 0.02923 for the greater and 0.00899 for the lesser.

The easiest mode of deformation of the acetonitrile oxide molecule is in the $E$ (trans) mode with respect to the CN bond, as previously observed for fulminic acid. We would note, however, that the methyl group makes the molecular motions slightly more difficult. A deformation of $10^{\circ}$ along the large axis (comprising $\Psi=9.2^{\circ}$ and $\Psi^{\prime}=3.9^{\circ}$ ) requires 0.9 kcal $\mathrm{mol}^{-1}$ and an analogous deformation along the small axis (comprising $\Psi=-3.9^{\circ}$ and $\Psi^{\prime}=9.2^{\circ}$ ) requires 2.92 kcal $\mathrm{mol}^{-1}$.
We have also studied the reaction pathway for the addition of water to acetonitrile oxide. In Figure 14 we have gathered the structural characteristics for the reactants, the transition state, and the reaction product. The energy of activation for addition is calculated as $29.2 \mathrm{kcal} \mathrm{mol}^{-1}$ and the heat of re-


Figure 13. Scheme for electronic rearrangement.


Figure 14. Structural characteristics for the reactants, products, and transition state for the addition of water to acetonitrile oxide.
action as $-78.3 \mathrm{kcal} \mathrm{mol}^{-1}$. Thus the addition of water to acetonitrile oxide has an activation energy which is significantly higher than that observed for the addition to fulminic acid. Thus the methyl group has an overall deactivating effect.

The deformation of the atoms of the acetonitrile oxide in going to the transition state calculated are $40^{\circ}$ for the angle $\Psi$ and $47^{\circ}$ for the angles $\Psi^{\prime}$ (as compared with 33 and $37^{\circ}$ for fulminic acid). Such a deformation of an isolated acetonitrile oxide requires $24.9 \mathrm{kcal} \mathrm{mol}^{-1}(E(40,47)-E(0,0))$. The parallel deformation of the water molecule (during which the angle changes from 100 to $109^{\circ}$ ) requires $2.3 \mathrm{kcal} \mathrm{mol}^{-1}$. Most (ca. 93\%) of the activation barrier consists of the energy required for the deformation of the isolated reactants as they approach the transition state. The difference between the activation barriers for the addition of water to fulminic acid and to acetonitrile oxide ( $5.7 \mathrm{kcal} \mathrm{mol}^{-1}$ ) is not due to the effect of the methyl group on the ease of deformation of the isolated reactants; in effect, in order to produce a deformation of $\Psi$ of $40^{\circ}$ and $\Psi^{\prime}$ of $47^{\circ}$ requires $24.8 \mathrm{kcal} \mathrm{mol}^{-1}$ for fulminic acid (as against $24.9 \mathrm{kcal} / \mathrm{mol}$ for $\mathrm{CH}_{3} \mathrm{CNO}$ ) and on the other hand $15.6 \mathrm{kcal} \mathrm{mol}^{-1}$ (against 15.5 ) is required to produce a deformation of $33^{\circ}$ for $\Psi$ and $37^{\circ}$ for $\Psi^{\prime}$. The influence of ease

Table VI. Overlap Populations, Bond Energies, and Degree of Evolution of Bonds at Several Points along the Reaction Pathway for the Water-Acetonitrile Oxide Reaction

|  | $\mathrm{O}_{1}-\mathrm{H}_{6}$ | $\mathrm{O}_{1}-\mathrm{C}_{2}$ | $\mathrm{C}_{2}-\mathrm{N}_{3}$ | $\mathrm{N}_{3}-\mathrm{O}_{4}$ | $\mathrm{O}_{4}-\mathrm{H}_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Overlap Populations |  |  |  |  |  |
| reactants | 0.2539 | 0.0000 | 0.7454 | 0.2115 | 0.0000 |
| transition state | 0.2721 | 0.0593 | 0.5844 | 0.2086 | 0.0089 |
| product | 0.0060 | 0.2773 | 0.4901 | 0.2193 | 0.2497 |
| Bond Energies (kcal mol ${ }^{-1}$ ) |  |  |  |  |  |
| reactants | 110.6 | 0.0 | 207.1 | 59.8 | 0.0 |
| transition state | 118.5 | 18.6 | 145.5 | 58.7 | 3.9 |
| product | 2.6 | 81.7 | 113.0 | 62.6 | 108.7 |
| Degree of Bond Evolution (\%) |  |  |  |  |  |
| $\underline{\text { transition state }}$ |  | 22.7 | 65.5 |  | 3.6 |

of deformation of the reactants (when both are deformed to the same extent) is thus very small indeed ( $0.1 \mathrm{kcal} \mathrm{mol}^{-1}$ ). The deactivating effect of the methyl group therefore probably arises from its electron-donating nature which tends to disfavor nucleophilic attack on the neighboring carbon; the transition state thus occurs later on the reaction coordinate, with a greater degree of deformation of the substrate.

This result is in line with experimental observations since the Hammett $\rho$ values for the attack of nucleophiles on the substituted benzonitrile oxides 2 are always positive (e.g., $\rho$

$=+0.57\left(\mathrm{H}_{2} \mathrm{O}\right.$ as nucleophile $),+0.80\left(\mathrm{HO}^{-}\right)$, and +0.75 $\left.\left(\mathrm{CH}_{3} \mathrm{CO}_{2}^{-}\right)\right)^{4}$ implying that electron donation reduces the reactivity.

In Table VI are noted the overlap populations, the energies, and the degrees of evolution of the bonds along the reaction pathway. The charge transfer measured on the basis of the Mulliken population is 0.16 to the transition state. One important point to note is that the intersystem bond $\mathrm{O}_{4} \mathrm{H}_{6}$, which is being formed, is more advanced in this case than for the reaction of fulminic acid. The asynchronization measured on this basis is $73 \%$. The reaction therefore remains concerted but strongly asynchronous, and proton transfer also occurs at or just after the transition state through the corridor (see Figure 11) with no energy barrier.

## Conclusions

The present work allows us to describe in some detail the mechanism of addition of water to fulminic acid and to acetonitrile oxide. The reaction is concerted (being overall $4 \pi+$ 2 s ) but highly asynchronous. The transfer of a proton from attacking water to the oxygen terminus of the 1,3 dipole begins at the transition state. This "proton slide" 19 is predicted to occur without an energy barrier. The product of addition is an oxime of the configuration $Z$ s-trans at the $\mathrm{O}_{1} \mathrm{C}_{2}$ bond and s-cis about the $\mathrm{N}_{3} \mathrm{O}_{4}$ bond. This form of hydroxyformaldoxime is not the most stable; obtained kinetically, it may evolve eventually to other ( $Z$ or $E$, different tautomeric) structures. However, such changes occur well after the transition state and do not affect our conclusions. The calculations also show the deactivating role of the $C$-methyl group, arising from steric
or electronic effects. It should be noted that the favorable internal proton transfer observed here may also occur either intermolecularly or via the intermediacy of other water molecules when the reaction is carried out in solution.

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## References and Notes

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